We claim:-

1. A process for preparing hyperbranched polymers which comprises reacting compounds of the formula I

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$$\begin{array}{c|c}
R^5 & R^2 & Z^1 \\
R^1 & R^3 \\
R^4 & Z^2
\end{array}$$

where

X is sulfur or oxygen,

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 R^1 and $R^3~$ are identical or different and are hydrogen, $C_1\text{-}C_6$ alkyl, $C_3\text{-}C_{12}$ cycloalkyl or $C_6\text{-}C_{14}$ aryl,

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 R^2 and R^4 are identical or different and are hydrogen, C_1 - C_6 alkyl, C_3 - C_{12} cycloalkyl, C_6 - C_{14} aryl,

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 Z^1 and Z^2 are identical or different and are COOH or COOR 6 , the radicals R^6 being identical or different and being C_1 - C_6 alkyl, formyl or CO- C_1 - C_6 alkyl,

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R⁵ identically or differently at each occurrence is C₁-C₆ alkyl or hydrogen, and

n is an integer from 2 to 10,

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optionally with at least one compound of the formula I a

$$\begin{array}{c|c}
R^5 & Z^1 \\
 & R^1 \\
 & R^1
\end{array}$$

Ιa

where the variables are as defined above,

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in the presence of a catalyst.

- 2. The process according to claim 1, wherein R¹ and R³ in formula I are identical.
- 3. The process according to claim 1 or 2, wherein R² and R⁴ in formula I are identical.

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- 4. The process according to any of claims 1 to 3, wherein Z¹ and Z² in formula I are each COOH.
- 5. The process according to any of claims 1 to 3, wherein Z¹ and Z² in formula I are each COOR⁶.
 - 6. The process according to any of claims 1 to 3 and 5, wherein the radicals R⁶ in formula I are each identical.
- The process according to any of claims 1 to 4, wherein R¹ and R³ in formula I are each identical and are methyl or hydrogen, R² and R⁴ in formula I are each hydrogen, and Z¹ and Z² in formula I are each COOR⁶.
- 8. The process according to any of claims 1 to 7, wherein from 0 to 1 000% by weight of compound of the formula I a are used, based on compound of the formula I.
 - 9. The process according to any of claims 1 to 8, wherein the reaction is carried out in the presence of at least one polyfunctional compound.

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- 10. The process according to any of claims 1 to 9, wherein the reaction is carried out in the presence of at least one enzyme.
- The process according to any of claims 1 to 9, wherein the reaction is carried out in the presence of an acidic inorganic, organometallic or organic catalyst or a mixture of two or more acidic inorganic, organometallic or organic catalysts.
 - A hyperbranched polymer obtainable by the process according to any of claims 1 to 11.

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13. A process for preparing hydrophilically modified hyperbranched polymers, which comprises reacting the hyperbranched polymer according to claim 12 with a hydrophilic compound.

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- 14. A hydrophilically modified hyperbranched polymer obtainable by the process according to claim 13.
- 15. A process for preparing hydrophobically modified hyperbranched polymers,
 which comprises reacting the hyperbranched polymer according to claim 12 with at least one hydrophobic alcohol.
 - 16. A hydrophobically modified hyperbranched polymer obtainable by the process according to claim 15.
 - 17. A process for preparing hyperbranched polymers modified with at least one ethylenically unsaturated compound, which comprises reacting the hyperbranched polymer according to claim 12 with at least one alcohol or amine which has an ethylenically unsaturated double bond.
 - 18. A hyperbranched polymer modified with at least one ethylenically unsaturated compound, obtainable by the process according to claim 17.
- 19. The use of the hyperbranched polymer according to claim 12 for producing an adhesive, coating, foam, covering, printing ink or varnish, especially a print varnish.
 - 20. A printing ink prepared using the hyperbranched polymer according to claim 12.
- 25 21. A print varnish prepared using the hyperbranched polymer according to claim 12 or using the hyperbranched polymer modified with at least one ethylenically unsaturated compound according to claim 18.